

Math 10A with Professor Stankova

Quiz 2; Wednesday, 9/6/2017

Section #107; Time: 11 AM

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Name: \_\_\_\_\_

Circle True or False or leave blank. (1 point for correct answer, -1 for incorrect answer, 0 if left blank)

1. True **FALSE** If  $f(x) = \sqrt{x}$ , then the domain of  $f^{-1}(x)$  is all real numbers.
2. True **FALSE** If  $f, g$  are functions such that  $\lim_{x \rightarrow 0} f(x) = L$  and  $g$  is continuous at  $x = L$ , then we must have  $\lim_{x \rightarrow 0} g(f(x)) = g(f(0))$ .

Show your work and justify your answers.

3. (10 points) Let  $f(t) = \frac{\sqrt{t+3} - 3}{t - 6}$ .

- (a) (2 points) What is the domain of  $f$ ?

**Solution:** The domain is when  $t + 3 \geq 0$  and  $t \neq 6$ . So the domain is  $D = [-3, \infty) \cap \{t : t \neq 6\} = [-3, 6) \cup (6, \infty) = \{t : t \geq -3 \text{ and } t \neq 6\}$ .

- (b) (3 points) Find  $\lim_{t \rightarrow 1} f(t)$ .

**Solution:** Since  $f$  is continuous at  $t = 1$ , which we know since it is a combination of polynomials, the limit is just  $f(1) = \frac{\sqrt{1+3} - 3}{1 - 6} = \frac{\sqrt{4} - 3}{-5} = \frac{1}{5}$ .

- (c) (5 points) Find  $\lim_{t \rightarrow 6} f(t)$ .

**Solution:** We have that

$$\begin{aligned} \lim_{t \rightarrow 6} \frac{\sqrt{t+3} - 3}{t - 6} &= \lim_{t \rightarrow 6} \frac{\sqrt{t+3} - 3}{t - 6} \cdot \frac{\sqrt{t+3} + 3}{\sqrt{t+3} + 3} \\ &= \lim_{t \rightarrow 6} \frac{t + 3 - 9}{(t - 6)(\sqrt{t+3} + 3)} = \lim_{t \rightarrow 6} \frac{1}{\sqrt{t+3} + 3} = \frac{1}{\sqrt{9} + 3} = \frac{1}{6}. \end{aligned}$$